

X-TUNE

Autotuning for Exascale: Self-Tuning Software to Manage Heterogeneity

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X-TUNE

Participants

	Current	Previous
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Argonne National Laboratory	Prasanna Balaprakash, Paul Hovland	Thomas Nelson (Colorado), Jeff Hammond, Sri Krishna Narayanan, Stefan Wild
USC/ISI		Jacqueline Chame



Which version would you prefer to write?

```

/* Laplacian 7-point Variable-Coefficient Stencil */
for (k=0; k<N; k++)
  for (j=0; j<N; j++)
    for (i=0; i<N; i++)
      temp[k][j][i] = b * h2inv * (
        beta_i[k][j][i+1] * ( phi[k][j][i+1] - phi[k][j][i] )
        -beta_i[k][j][i] * ( phi[k][j][i] - phi[k][j][i-1] )
        +beta_j[k][j+1][i] * ( phi[k][j+1][i] - phi[k][j][i] )
        -beta_j[k][j][i] * ( phi[k][j][i] - phi[k][j-1][i] )
        +beta_k[k+1][j][i] * ( phi[k+1][j][i] - phi[k][j][i] )
        -beta_k[k][j][i] * ( phi[k][j][i] - phi[k-1][j][i] ) );

/* Helmholtz */
for (k=0; k<N; k++)
  for (j=0; j<N; j++)
    for (i=0; i<N; i++)
      temp[k][j][i] = a * alpha[k][j][i] * phi[k][j][i] -
        temp[k][j][i];

/* Gauss-Seidel Red Black Update */
for (k=0; k<N; k++)
  for (j=0; j<N; j++)
    for (i=0; i<N; i++){
      if ((i+j+k+color)%2 == 0 )
        phi[k][j][i] = phi[k][j][i] - lambda[k][j][i] *
          (temp[k][j][i] - rhs[k][j][i]);}

```

```

int planeInWaveFront; for (planeInWaveFront=0; planeInWaveFront<ghosts.planeInWaveFront; planeInWaveFront++)
  global_lj_end[planeInWaveFront] = C[planeInWaveFront]*pencil
  global_lj_end[planeInWaveFront] = C[ghosts.dims+ghosts-1]*planeInWaveFront+2*pencil
  lj_start[planeInWaveFront] = global_lj_end[planeInWaveFront];
  lj_end[planeInWaveFront] = global_lj_end[planeInWaveFront];
...
int i;
for (i=0; i<N; i++)
  for (j=0; j<N; j++)
    for (k=0; k<N; k++)
      phi[k][j][i] = a * alpha[k][j][i] * phi[k][j][i] -
        temp[k][j][i];

/* Gauss-Seidel Red Black Update */
for (k=0; k<N; k++)
  for (j=0; j<N; j++)
    for (i=0; i<N; i++){
      if ((i+j+k+color)%2 == 0 )
        phi[k][j][i] = phi[k][j][i] - lambda[k][j][i] *
          (temp[k][j][i] - rhs[k][j][i]);}

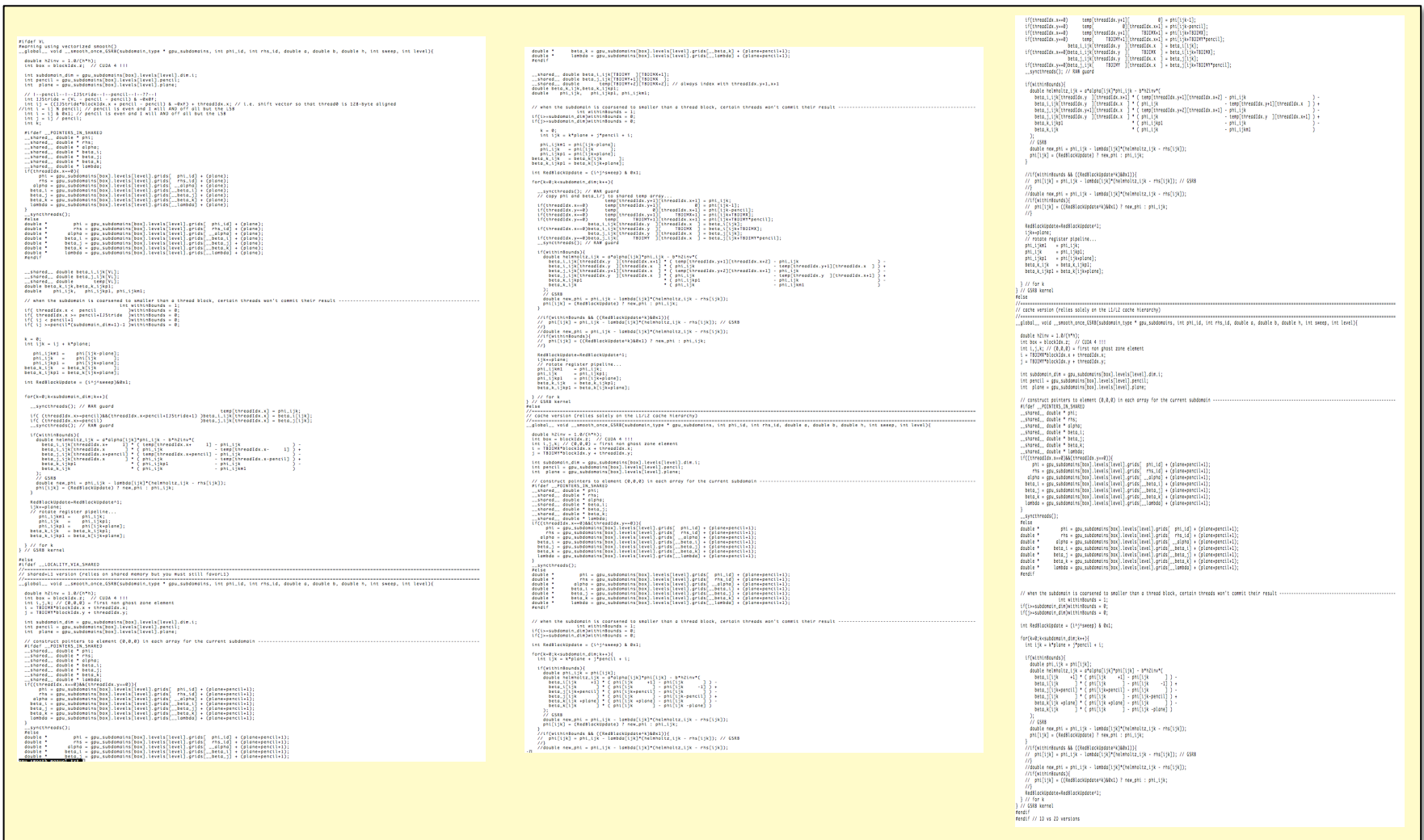
```

Code A: miniGMG baseline smooth operator approximately 13 lines of code

Code B: miniGMG optimized smooth operator approximately 170 lines of code



And now GPU code?



Code C: miniGMG optimized smooth operator for GPU, 308 lines of code for just kernel



Which version would you prefer to write?

```
/* local_grad_3 computation from nek5000 */
w[nelt i j k] += Dt[I k] U[nelt n m l] D[j m] D[i n]
```

Code A:

1 line mathematical representation
Input to OCTOPI

```
/* local_grad3 from nek5000, generated CUDA code */
```

```
void local_grad3(double *U,double *ur,double *us,double *Dt,double *ut,double *D){
    double *devI1Prt;
    double *devO3Prt;
    double *devO2Prt;
    double *devO1Prt;
    double *devI2Prt;
    double *devI3Prt;

    struct timeval time1, time2;
    double time;
    std::ofstream timefile;
    std::ofstream Mlsearchfile;

    cudaMalloc((void **)&devI1Prt,100 * sizeof(double ));
    cudaMalloc((void **)&devI2Prt,1000000 * sizeof(double ));
    cudaMalloc((void **)&devI3Prt,100 * sizeof(double ));
    cudaMalloc((void **)&devO1Prt,1000000 * sizeof(double ));
    cudaMalloc((void **)&devO2Prt,1000000 * sizeof(double ));
    cudaMalloc((void **)&devO3Prt,1000000 * sizeof(double ));

    cudaMemcpy(devI1Prt,D,100 * sizeof(double ),cudaMemcpyHostToDevice);
    cudaMemcpy(devI2Prt,U,1000000 * sizeof(double ),cudaMemcpyHostToDevice);
    cudaMemcpy(devI3Prt,Dt,100 * sizeof(double ),cudaMemcpyHostToDevice);

    dim3 dimGrid0 = dim3(1000,10);
    dim3 dimBlock0 = dim3(10,10);

    gettimeofday(&time1, 0);
    local_grad_3_GPU_0<dimGrid0,dimBlock0>>(devI1Prt,devO1Prt,devO3Prt,devI3Prt,devI2Prt,devI3Prt);
    gettimeofday(&time2, 0);

    time = (1000000.0*(time2.tv_usec-time1.tv_usec) + time2.tv_usec-time1.tv_usec)/1000000.0;
    timefile.open("fines/time_10_k_nelt_n.txt", std::ofstream::out | std::ofstream::app );
    timefile << time << endl;
    timefile.close();
    Mlsearchfile.open("fines/Mlsearchfile_10_k_nelt_n.txt", std::ofstream::out | std::ofstream::app );
    Mlsearchfile << "local_grad_3 " << "time" << time << " [f_0] 10 [PERRATE_0_T0] k [PERRATE_0_B0] nelt  
se_orio_chi_10_k_nelt_n_cu" << endl;
    Mlsearchfile.close();

    cudaMemcpy(ur,devO1Prt,1000000 * sizeof(double ),cudaMemcpyDeviceToHost);
    cudaMemcpy(us,devO2Prt,1000000 * sizeof(double ),cudaMemcpyDeviceToHost);
    cudaMemcpy(ut,devO3Prt,1000000 * sizeof(double ),cudaMemcpyDeviceToHost);

    cudaFree(devI1Prt);
    cudaFree(devO3Prt);
    cudaFree(devO2Prt);
    cudaFree(devO1Prt);
    cudaFree(devI2Prt);
    cudaFree(devI3Prt);
}

__global__ void local_grad_3_GPU_0<double *ur,double *us,double *ut,double *D,double *U,double *Dt>
{
    int bx;
    double newVariable0;
    double newVariable1;
    double newVariable2;
    bx = blockIdx.x;
    int by;
    by = blockIdx.y;
    int tx;
    tx = threadIdx.x;
    int ty;
    ty = threadIdx.y;
    int t4;
    int t6;
    int t8;
    int t10;
    newVariable0 = ur[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + ty];
    newVariable1 = us[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + ty];
    newVariable2 = ut[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + ty];
    newVariable0 = newVariable0 + D[0 * 10 + ty] * U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + 0];
    newVariable1 = newVariable1 + U[bx * 10 * 10 * 10 + by * 10 * 10 + 0 * 10 + ty] * Dt[tx * 10 + 0];
    newVariable2 = newVariable2 + U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + ty] * Dt[by * 10 + 0];
    newVariable0 = newVariable0 + D[(0 + 1) * 10 + ty] * U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + (0 + 1)];
    newVariable1 = newVariable1 + U[bx * 10 * 10 * 10 + by * 10 * 10 + (0 + 1) * 10 + ty] * Dt[tx * 10 + (0 + 1)];
    newVariable2 = newVariable2 + U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + ty] * Dt[by * 10 + (0 + 1)];
    newVariable0 = newVariable0 + D[(0 + 2) * 10 + ty] * U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + (0 + 2)];
    newVariable1 = newVariable1 + U[bx * 10 * 10 * 10 + by * 10 * 10 + (0 + 2) * 10 + ty] * Dt[tx * 10 + (0 + 2)];
    newVariable2 = newVariable2 + U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + ty] * Dt[by * 10 + (0 + 2)];
    newVariable0 = newVariable0 + D[(0 + 3) * 10 + ty] * U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + (0 + 3)];
    newVariable1 = newVariable1 + U[bx * 10 * 10 * 10 + by * 10 * 10 + (0 + 3) * 10 + ty] * Dt[tx * 10 + (0 + 3)];
    newVariable2 = newVariable2 + U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + ty] * Dt[by * 10 + (0 + 3)];
    newVariable0 = newVariable0 + D[(0 + 4) * 10 + ty] * U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + (0 + 4)];
    newVariable1 = newVariable1 + U[bx * 10 * 10 * 10 + by * 10 * 10 + (0 + 4) * 10 + ty] * Dt[tx * 10 + (0 + 4)];
    newVariable2 = newVariable2 + U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + ty] * Dt[by * 10 + (0 + 4)];
    newVariable0 = newVariable0 + D[(0 + 5) * 10 + ty] * U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + (0 + 5)];
    newVariable1 = newVariable1 + U[bx * 10 * 10 * 10 + by * 10 * 10 + (0 + 5) * 10 + ty] * Dt[tx * 10 + (0 + 5)];
    newVariable2 = newVariable2 + U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + ty] * Dt[by * 10 + (0 + 5)];
    newVariable0 = newVariable0 + D[(0 + 6) * 10 + ty] * U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + (0 + 6)];
    newVariable1 = newVariable1 + U[bx * 10 * 10 * 10 + by * 10 * 10 + (0 + 6) * 10 + ty] * Dt[tx * 10 + (0 + 6)];
    newVariable2 = newVariable2 + U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + ty] * Dt[by * 10 + (0 + 6)];
    newVariable0 = newVariable0 + D[(0 + 7) * 10 + ty] * U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + (0 + 7)];
    newVariable1 = newVariable1 + U[bx * 10 * 10 * 10 + by * 10 * 10 + (0 + 7) * 10 + ty] * Dt[tx * 10 + (0 + 7)];
    newVariable2 = newVariable2 + U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + ty] * Dt[by * 10 + (0 + 7)];
    newVariable0 = newVariable0 + D[(0 + 8) * 10 + ty] * U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + (0 + 8)];
    newVariable1 = newVariable1 + U[bx * 10 * 10 * 10 + by * 10 * 10 + (0 + 8) * 10 + ty] * Dt[tx * 10 + (0 + 8)];
    newVariable2 = newVariable2 + U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + ty] * Dt[by * 10 + (0 + 8)];
    newVariable0 = newVariable0 + D[(0 + 9) * 10 + ty] * U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + (0 + 9)];
    newVariable1 = newVariable1 + U[bx * 10 * 10 * 10 + by * 10 * 10 + (0 + 9) * 10 + ty] * Dt[tx * 10 + (0 + 9)];
    newVariable2 = newVariable2 + U[bx * 10 * 10 * 10 + by * 10 * 10 + tx * 10 + ty] * Dt[by * 10 + (0 + 9)];
    ur[by * 10 * 10 * 10 + bx * 10 * 10 + tx * 10 + ty] = newVariable1;
    ut[by * 10 * 10 * 10 + bx * 10 * 10 + tx * 10 + ty] = newVariable2;
}
```

Code B:

Generated CUDA+harness, 122 lines of code



Exascale Challenges: Code B is not Unusual

- Performance portability?
 - Particularly across fundamentally different CPU and GPU architectures
- Programmer productivity?
 - High performance implementations will require low-level specification that exposes architecture
- Software maintainability and portability?
 - May require multiple implementations of application

Current solutions

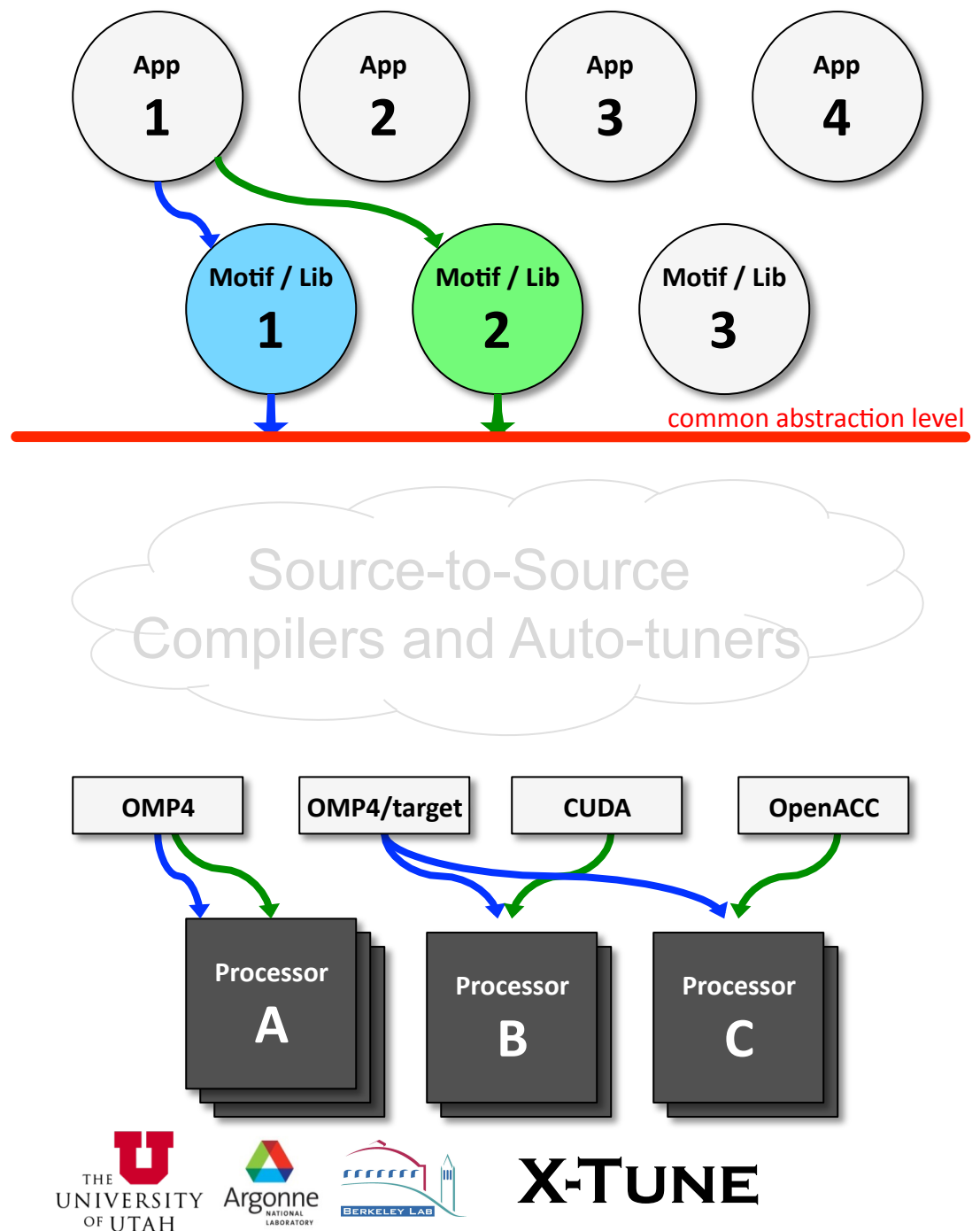
- Follow MPI and OpenMP standards
 - Same code unlikely to perform well across CPU and GPU
 - Vendor C and Fortran compilers not optimized for HPC workloads
- Some domain-specific framework strategies
 - Libraries, C++ template expansion, standalone DSL
 - Not *composable* with other optimizations



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Programming Systems Must Hide Complexity!

- Define a common abstraction(s) that programmers can target
 - hide **programming model choices** from users
 - hide **architectural complexity** from users
 - hide **tuning** from users
- Use compilation tools to map to optimal implementation



X-TUNE Goals

- Application programmer expresses key computation at a high level (**Code A**)
 - Sequential C or domain-specific specification
- Code transformations are applied
 - Existing and domain-specific transformations
 - Generates a collection of optimized implementations
 - Includes thread-level code generation (OpenMP and CUDA)
- Autotuning
 - Searches the space of implementations to find the best match to execution context
 - Selects optimized implementation (**Code B**)
- Automation mitigates correctness, productivity, portability, maintainability concerns

***X-TUNE automates the process of converting Code A to Code B.
See today's demonstrations!***

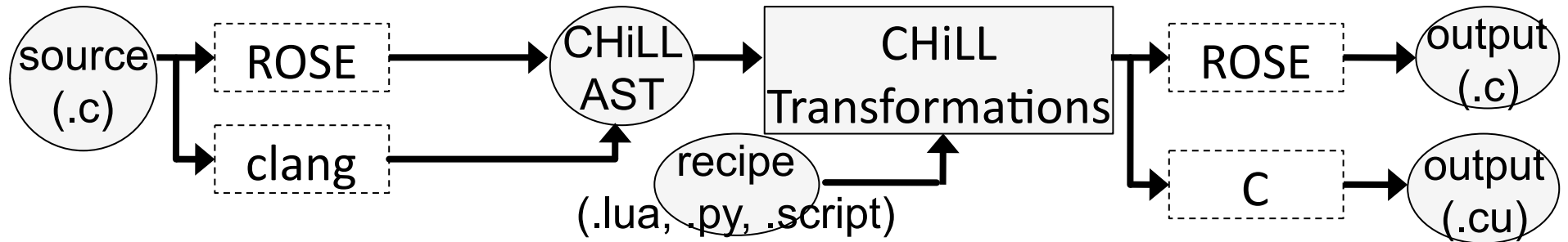


X-TUNE

X-TUNE Approach

- For each *motif*, start with manually-tuned code or work with developer of new code
 - What transformations are needed to target specific architectures?
 - What performance questions can be addressed by autotuning?
- Attempt to automate
 - Exploit existing compiler transformations
 - Develop new domain-specific transformations and required analysis and code generation support
 - Develop decision algorithms
- Collect application code from collaborators, Co-Design Centers and other DOE application teams
 - Generalize from experiments with manually-tuned code

X-TUNE Key Ideas



CUDA-CHiLL

- **Composable** transformation and code generation
 - Leverage rich set of existing transformations and code generation capability in **polyhedral framework**
- Extensible to domain-specific transformations and decision algorithms
 - **Compose** with existing transformations
- Optimization strategies and parameters exposed to autotuning via transformation recipes
- Search space navigation
 - Search framework can be standalone tool (e.g., Orio, OpenTuner, Active Harmony, Nitro)

Example Motifs Supported by X-TUNE

Motif	Input	Existing Transformations	Domain-specific transformations	Autotuning	Search
Geometric Multigrid	Sequential C computation (w/ MPI and OpenMP harness)	Communication-avoiding: fusion, tile, wavefront (skew&permute), OpenMP, CUDA	Ghost zones, Partial sums	Ghost zone depth, threading, strategy at each level of V-cycle	Simple, full space
Tensor Contraction	Mathematical Formula	Tile, permute, scalar replacement, unroll, CUDA	Rewriting, Decision algorithm	Loop order, CUDA threading	SURF
Sparse Matrix Computation	Sequential C with CSR matrix	Tile, permute, skew, unroll, reduction, scalar expansion, OpenMP, CUDA	Generate inspectors, coalesce, make-dense, compact, split, level sets	Threading, matrix repr.	Simple, full space

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DEMO

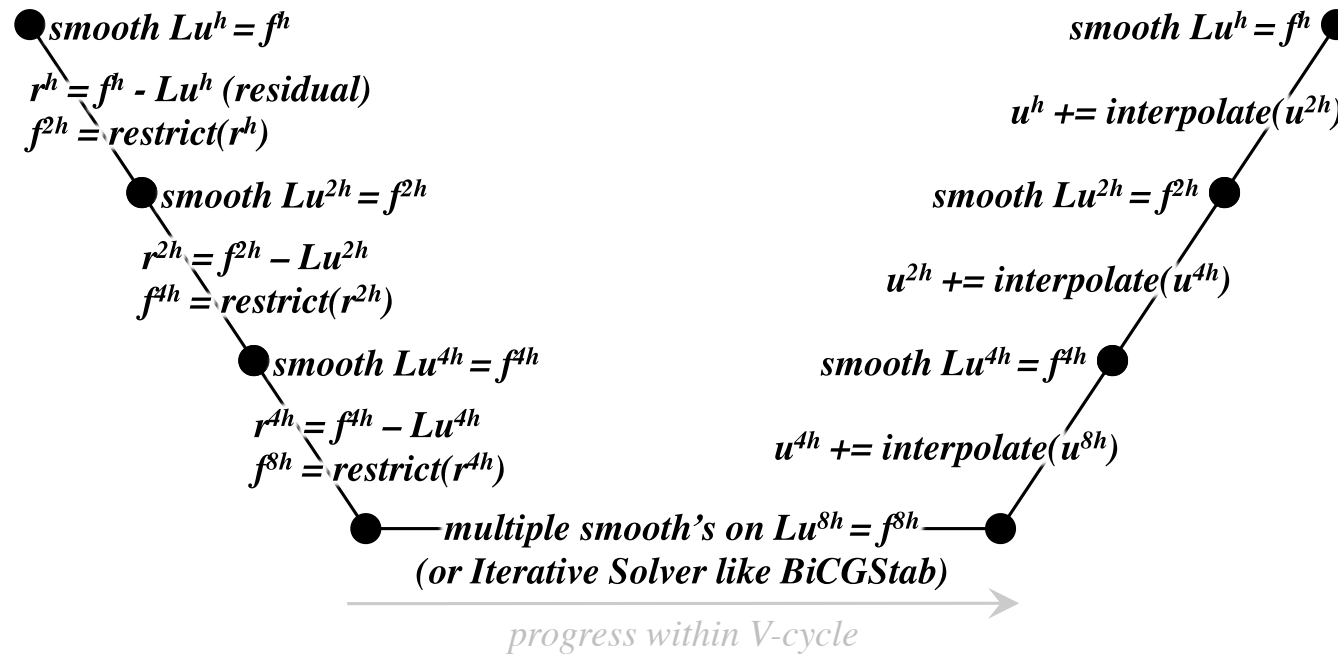
SUPER/NSF



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Geometric Multigrid

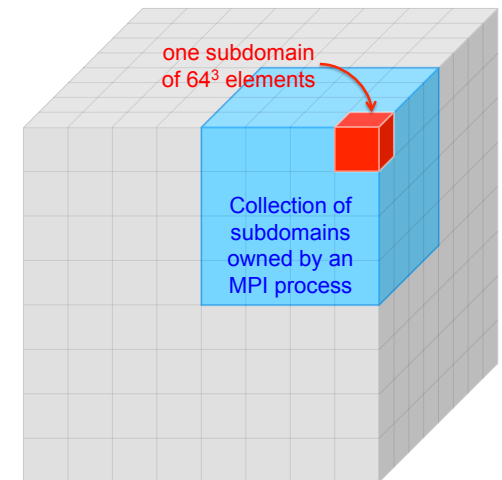
- Multigrid solves elliptic PDEs in $O(N)$ computational complexity by using a hierarchical approach.



- ❖ Geometric Multigrid (**GMG**) is specialization in which the operator (A) is simply a stencil on a structured grid (i.e. *matrix-free*)
- ❖ Stresses performance at different degrees of parallelism, locality, working set sizes, etc...
- ❖ Optimization strategy varies across different levels of V-cycle, even on one architecture!

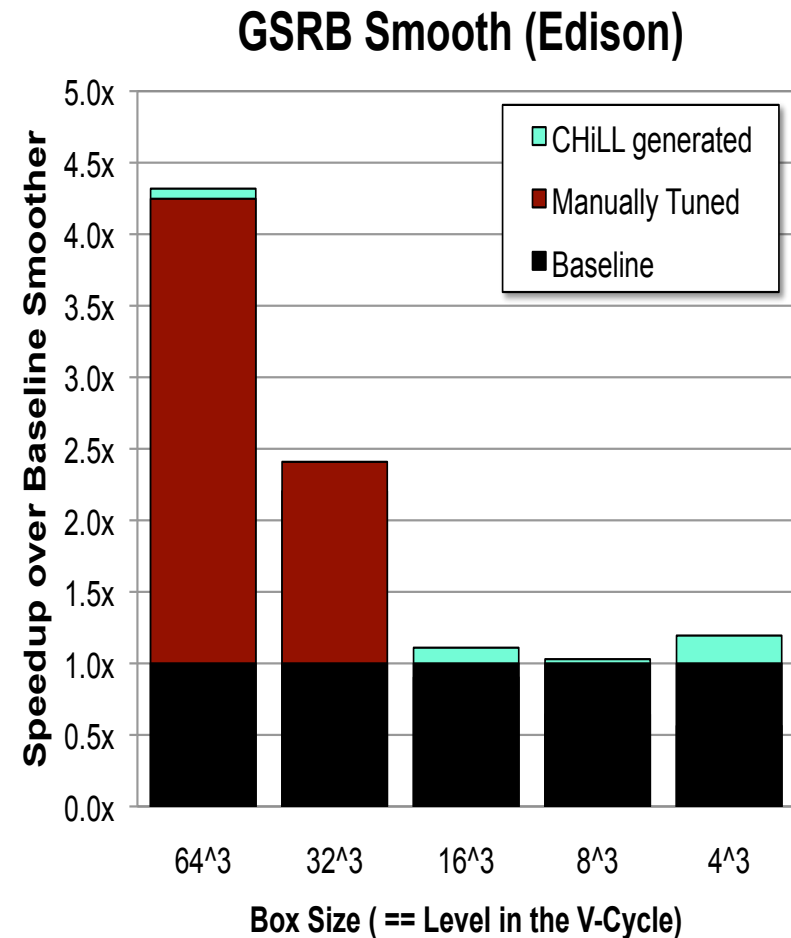
miniGMG Benchmark

- **miniGMG proxies the MG solves in BoxLib/Chombo codes**
 - Predecessor to ExACT Co-Design Center's HPGMG
- Distributed memory (MPI) implementation
- **operator** is configurable
 - 7pt variable coefficient **proxies LMC**
 - 7pt constant coefficient is simpler
 - 125pt/27pt/13pt high-order stencils
- **smoother** in the v-cycle is configurable
 - Gauss Seidel, Red-Black (GSRB) = **proxies**
 - Jacobi (mathematically weaker)
- **bottom solver** is configurable
 - multiple GSRB's
 - Krylov solver like **BiCGStab**, CG, CA-BiCGStab, CA-CG, etc...



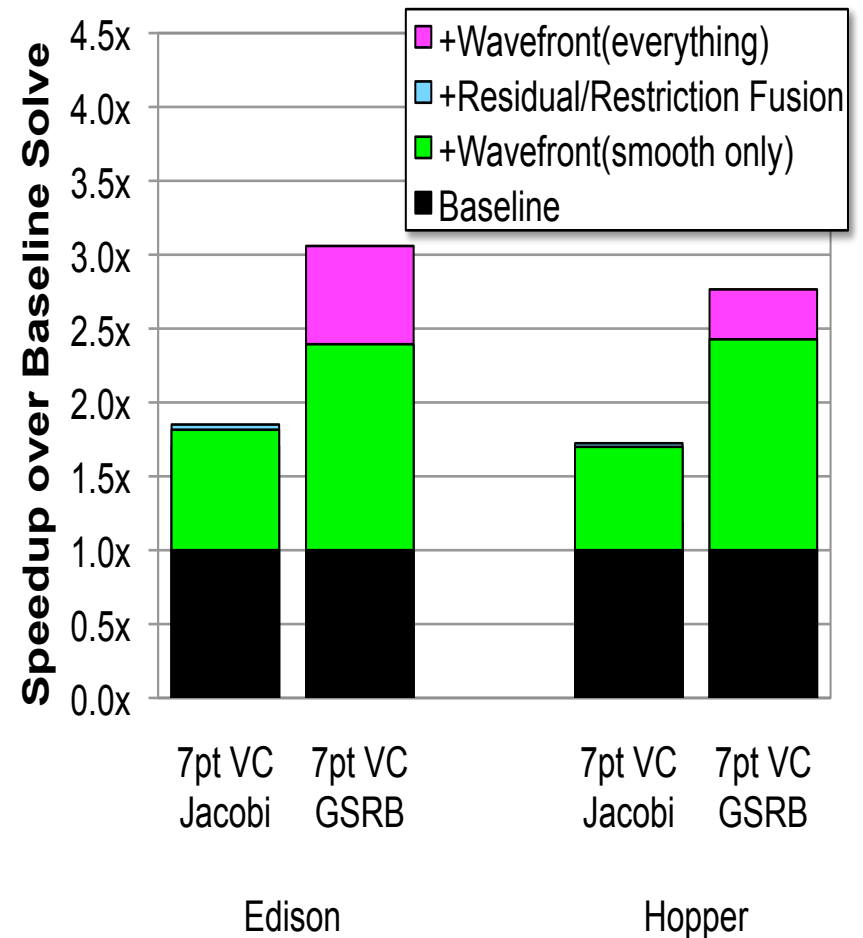
Optimized Code A can beat Code B!

- miniGMG optimized w/CHiLL
 - fused operations
 - created a communication-avoiding wavefront
 - **auto-parallelized (OpenMP)**
- **autotuning** finds the best implementation for each box size
 - wavefront depth (degree of comm. avoiding)
 - Turn on/off optimizations (fusion, wavefront)
 - nested OpenMP configuration
 - inter-thread synchronization (barrier vs. P2P)
- For fine grids (large arrays) CHiLL attains a **4.3x speedup** over baseline



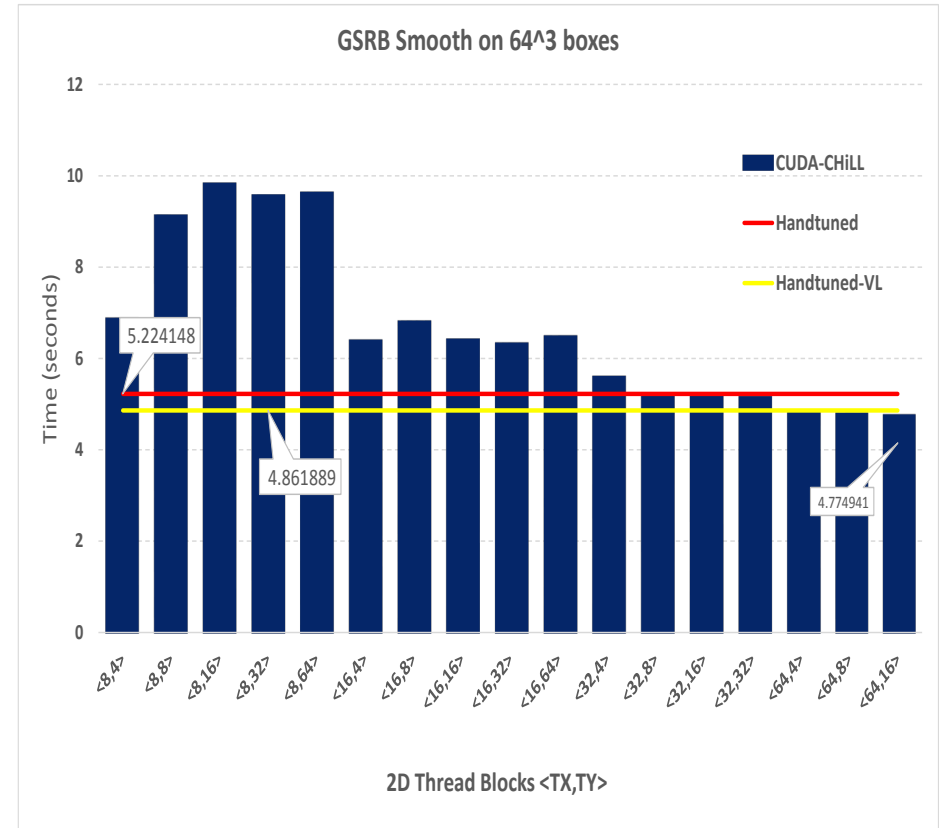
Flexibility

- Fuse the residual and restriction operations into the wavefront as well
 - read u^h , R^h , and coefficients once
 - perform 4 smooths (**no additional data movement**)
 - write smoothed u^h and new R^{2h}
- Apply these transformations to a different smoother and autotune it
 - up to **3x improvement in MGSolve**



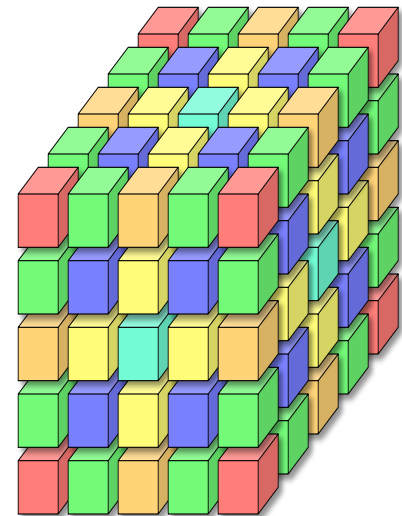
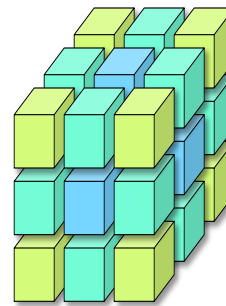
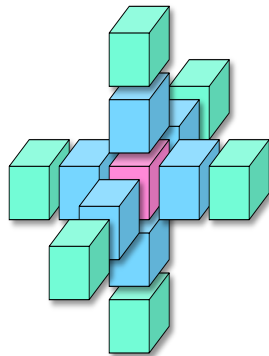
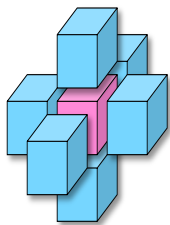
Retargetable and Performance Portable: Optimized Code A can beat Code C!

- CHiLL can obviate the need for architecture-specific programming models like CUDA
 - CUDA-CHiLL took the sequential GSRB implementation (.c) and **generated CUDA** that runs on NVIDIA GPUs
 - CUDA-CHiLL tunes for the current target machine whereas static implementations hand-optimize for yesterday's GPUs
 - CUDA-CHiLL autotuned over the thread block sizes and is ultimately **2% faster** than the hand-optimized minimg-cuda (**Code C**)



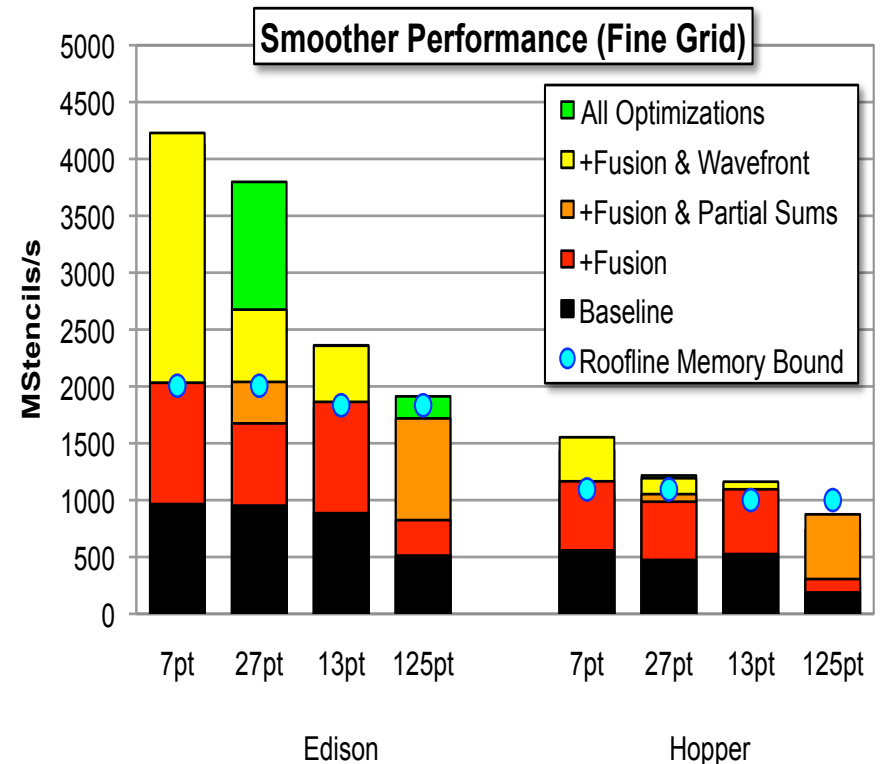
Extensible to Domain-Specific Optimizations

- Applied mathematicians are exploring how changing the stencils may be better suited for future architecture trends
- Consider the following variations (stencils) on the discretization of the Laplacian
 - low-level implementations (optimized OMP4) may provide high performance
 - but are one-off solutions as requisite optimizations/tuning change from one stencil to the next



Extensible to Domain-Specific Optimizations

- CHiLL optimized/tuned each of these stencils
 - Introduced **partial sums** optimization to avoid redundant computation for compute-bound high-order stencils
 - selected unique optimizations for each stencil and at each level of the MG V-Cycle
 - Without a communication-avoiding wavefront, CHiLL delivered performance **near the Roofline bound**.
 - Using a wavefront, CHiLL can nearly **double** the nominal Roofline performance for the 7- and 27-point operators.



Example Transformation Recipes

- These can be manually-written (miniGMG) or automatically generated (tensor contraction)

```
/* jacobi_box_4_64.py, 27-pt stencil, 643 box size */
from chill import *

#select which computation to optimize
source('jacobi_box_4_64.c')
procedure('smooth_box_4_64')
loop(0)
original() # fuse wherever possible

#create a parallel wavefront
skew([0,1,2,3,4,5],2,[2,1])
permute([2,1,3,4])

#partial sum for high order stencils and fuse result
distribute([0,1,2,3,4,5],2)
stencil_temp(0)
stencil_temp(5)
fuse([2,3,4,5,6,7,8,9],1)
fuse([2,3,4,5,6,7,8,9],2)
fuse([2,3,4,5,6,7,8,9],3)
fuse([2,3,4,5,6,7,8,9],4)
```

```
/* gsrub.lua, variable coefficient GSRB, 643 box size */
init("gsrb_mod.cu", "gsrb",0,0)
dofile("cudaize.lua") # custom commands in lua

# set up parallel decomposition, adjust via autotuning
TI=32
TJ=4
TK=64
TZ=64

tile_by_index(0, {"box","k","j","i"},{TZ,TK, TJ, TI},
{I1_control="bb", I2_control="kk", I3_control="jj",
I4_control="ii"},{"bb","box","kk","k","jj","j","ii","i"})

cudaize(0, "kernel_GPU",
{ _temp=N*N*N*N, _beta_i=N*N*N*N,
_phi=N*N*N*N},{block={"ii","jj","box"},
thread={"i","j"}},{ })
```

Tensor Contraction: Spectral Element Method from nek5000/nekbone (CESAR)

$$C = A \otimes B \underline{u}$$

- A and B are square matrices
- \underline{u} is a component vector
- In 2-d, C can be computed:

$$c_{i,j} = \sum_l \sum_k a_{j,l} b_{i,k} u_{k,l}$$

Order $O(n^4)$

Optimize by rewriting to the following:

$$C = (A \otimes I)(I \otimes B)\underline{u}$$

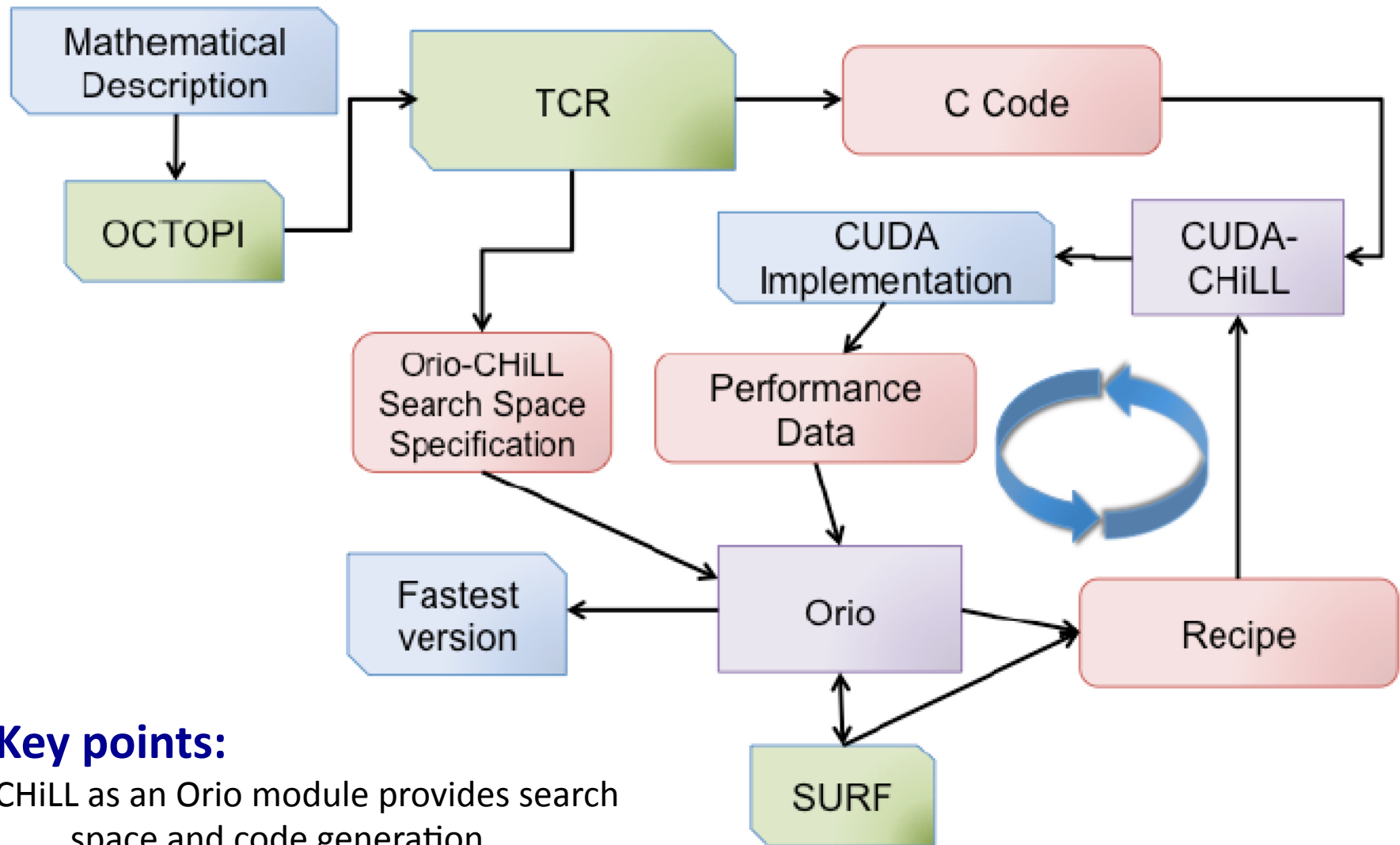
Partial Results: $\underline{w} = (I \otimes B)\underline{u} \longrightarrow w_{i,j} = \sum_l u_{i,l} b_{l,j}^T$ Order $O(n^3)$

Final Results: $C = (A \otimes I)\underline{w} \longrightarrow c_{i,j} = \sum_k a_{i,k} w_{k,j}$

Tensor Contraction: Challenging Mapping, Particularly for GPU

- What is the optimal contraction order?
- What is the optimal loop order? (N! different implementations)
- GPU challenges: small dimensions, memory hierarchy effects
- Search space is discontinuous, noisy, and expensive to evaluate
- X-TUNE Approach:
 - Fully automate from mathematical description to GPU code generation (**Code A** to **Code B**)
 - Automate and reduce search time across intractable brute force search space

Baracuda Framework



Key points:

CHiLL as an Orio module provides search space and code generation

SURF manages exploration of search space



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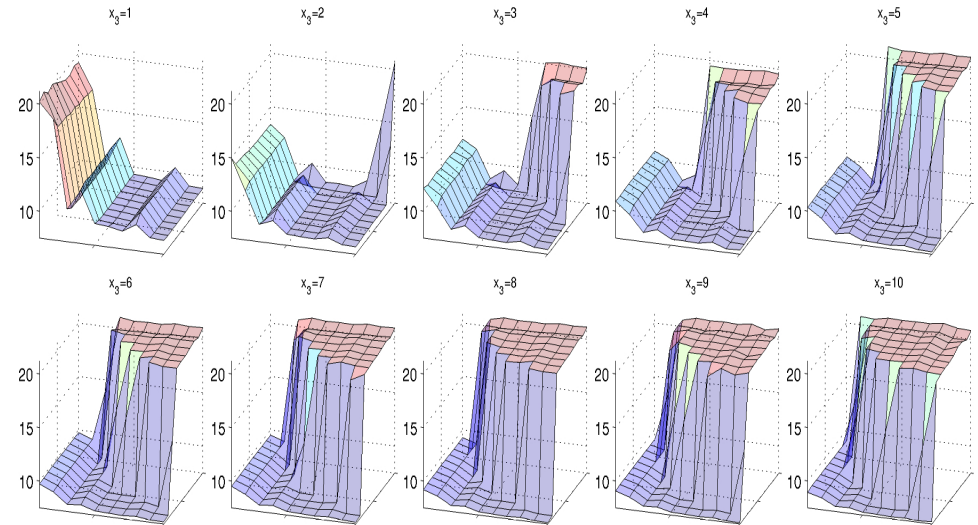
SURF: Model-Based Search

■ Search Using Random Forests

- state-of-the-art statistical machine learning algorithm
- handles binary permutation parameters
- handles nonlinear parameter interactions

■ Approach

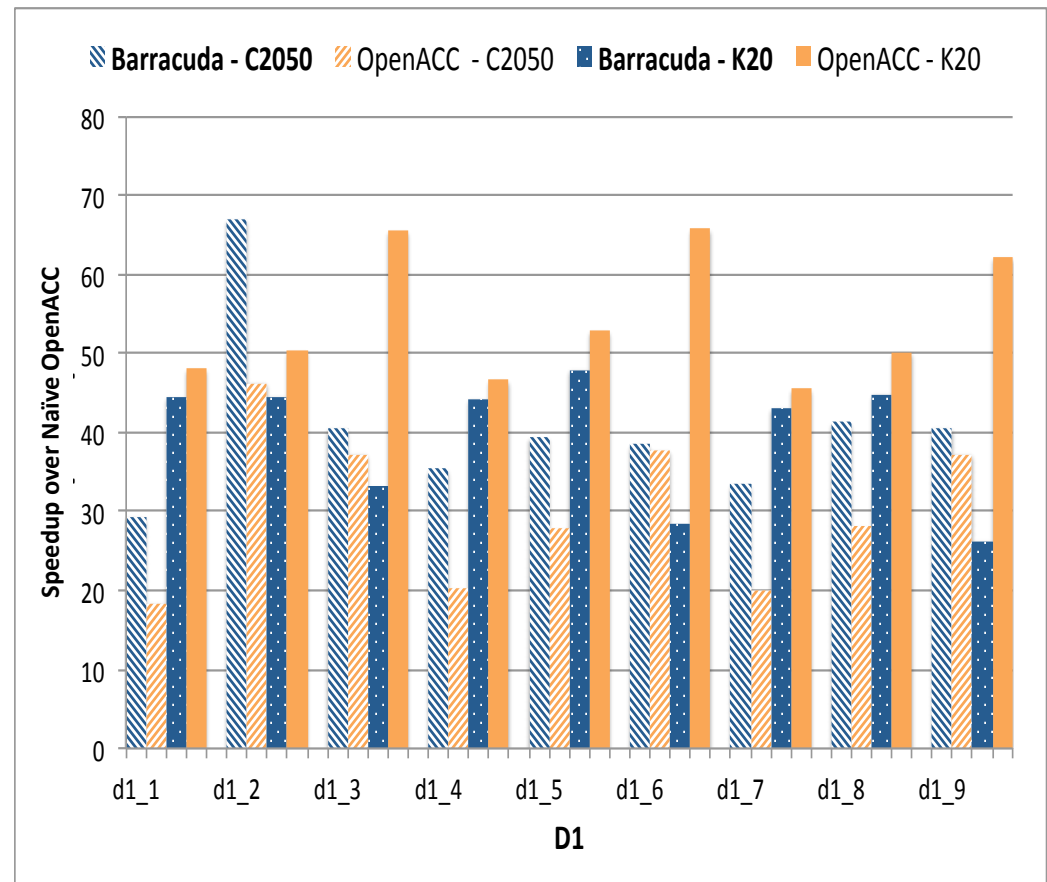
- start with promising small set of parameter configurations
- evaluate performance
- fit surrogate model (ML)
- predict new set of high-performing configurations
- iterate



*Example Surrogate Model Fitted to Sampled Performance
(iterative refinement improves the statistical model)*

Optimizing NWChem

- Extracted representative on-node tensor contractions from NWChem/TCE
 - many small contractions
 - atypical of OpenACC use model
- Baracuda generates optimized CUDA for NVIDIA's Fermi or Kepler GPUs
- Manually modified CUDA to OpenACC
 - Naïve replaces CUDA with OpenACC, but uses same loop order and parallelization
 - OpenACC = naïve + manual explicit control over hierarchical parallelism



Optimizing Nekbone

- Nekbone (CESAR CoDesign Center Proxy App) with optimized local_grad_3 and local_grad_3t
 - Many, small (e.g. 12x12x12) contractions
 - Nominally implemented as many BLAS3 calls
- Baracuda generates optimized CUDA for NVIDIA's Fermi or Kepler GPUs
- Compare to single Haswell core.

Speedup over 1-core Haswell	Naïve OpenACC	Optimized OpenACC	Baracuda (CUDA)
K20	2.86	12.39	36.47
C2050	1.18	19.21	34.65

Summary of X-TUNE Accomplishments

- Demonstrated for two motifs, Geometric Multigrid and Tensor Contraction
 - Automated architecture-specific optimization from high-level specification
 - Performance rivaling manually-tuned code and sometimes better
 - Approach can achieve performance portability, productivity and maintainability
- Implementation status
 - GMG optimizations integrated into CHiLL, tensor contraction uses existing CHiLL with additional frontend and Orio
 - CHiLL publicly available on github
 - Installed on Edison (user space)
 - Demonstrations this evening



X-TUNE

Publications

- Papers

- P. Basu, M. Hall, M. Khan, S.Maindola, S.Muralidharan, S.Ramalingam, A.Rivera, M.Shantharam, A.Venkat. Towards Making Autotuning Mainstream. International Journal of High Performance Computing Applications, 27(4), November 2013.
- P. Basu, S. Williams, A. Venkat, B. Van Straalen, M. Hall, and L. Oliker. Compiler generation and autotuning of communication-avoiding operators for geometric multigrid. In High Performance Computing Conference (HIPC), 2013.
- P. Basu, S. Williams, A. Venkat, B. Van Straalen, M. Hall, and L. Oliker. Compiler generation and autotuning of communication-avoiding operators for geometric multigrid. In Workshop on Optimizing Stencil Computations (WOSC), 2013.
- Protonu Basu, Samuel Williams, Brian Van Straalen, Mary Hall, Leonid Oliker, Phillip Colella, "Compiler-Directed Transformation for Higher-Order Stencils", International Parallel and Distributed Processing Symposium (IPDPS), May 2015.
- Thomas Nelson, Axel Rivera, Prasanna Balaprakash, Mary Hall, Paul D. Hovland, Elizabeth Jessup, Boyana Norris, "Generating Efficient Tensor Contractions for GPUs", International Conference on Parallel Processing (ICPP), September 2015.

- Thesis and Dissertations

- Axel Rivera. Using Autotuning for Accelerating Tensor-Contraction on GPUs, Masters thesis, University of Utah, December 2014.
- Protonu Basu, "Compiler Optimizations and Autotuning for Stencils and Geometric Multigrid", PhD Dissertation, University of Utah, December 2015.
- Thomas Nelson, "DSLs and Search for Linear Algebra Performance Optimization," PhD Dissertation, University of Colorado, December 2015.